

# Mathematical Processes Standard

*Students use mathematical processes and knowledge to solve problems. They apply the mathematical processes as they learn content from the other mathematical standards.*

Grade 1 Indicators	Grade 2 Indicators	Grade 3 Indicators
<p><b><u>Problem Solving</u></b></p> <p>1. Apply and adapt a variety of appropriate strategies to solve problems: draw a picture</p> <ul style="list-style-type: none"> <li>• create a mathematical model</li> <li>• draw a picture</li> <li>• act it out</li> <li>• look for a pattern</li> <li>• guess and check</li> </ul> <p><b><u>Reasoning and Proof</u></b></p> <p>1. Use models and logic to make conclusions. 2. Adjust models as needed. 3. Reason inductively by identifying patterns.</p> <p><b><u>Communication</u></b></p> <p>1. Use developmentally appropriate mathematical vocabulary. 2. Respond to instructions orally, and visually as appropriate; e.g., tell, share, describe, demonstrate, compare. 3. Respond clearly with sufficient detail so that Thinking can be understood.</p> <p><b><u>Connections</u></b></p> <p>1. Use learning from one area of mathematics to understand another. 2. Relate new and prior knowledge to make sense of new concepts being learned. 3. Make connections between mathematics and everyday life.</p> <p><b><u>Representation</u></b></p> <p>1. Select an appropriate representation of a mathematical idea or situation:</p> <ul style="list-style-type: none"> <li>• physical model/manipulative</li> <li>• picture/drawing</li> <li>• numerical</li> <li>• geometric</li> </ul>	<p><b><u>Problem Solving</u></b></p> <p>1. Apply and adapt a variety of appropriate strategies to solve problems:</p> <ul style="list-style-type: none"> <li>• create a mathematical model</li> <li>• draw a picture</li> <li>• act it out</li> <li>• look for a pattern</li> <li>• guess and check</li> <li>• make an organized list</li> </ul> <p><b><u>Reasoning and Proof</u></b></p> <p>1. Use models and logic to make conclusions. 2. Adjust models as needed. 3. Reason inductively by identifying patterns. 4. Evaluate and analyze the mathematical thinking and strategies of others orally.</p> <p><b><u>Communication</u></b></p> <p>1. Use developmentally appropriate mathematical vocabulary. 2. Respond to instructions orally, visually and in writing as appropriate; e.g., tell, share, describe, demonstrate, compare, discuss, write. 3. Respond clearly with sufficient detail so that thinking can be understood. 4. Present thinking in a logical and organized in manner and explain to others how a problem was solved.</p> <p><b><u>Connections</u></b></p> <p>1. Use learning from one area of mathematics to understand another. 2. Relate new and prior knowledge to make sense of new concepts being learned. 3. Make connections between mathematics and everyday life. 4. Apply a strategy or reference system that draws on previous learning in another context.</p>	<p><b><u>Problem Solving</u></b></p> <p>1. Apply and adapt a variety of appropriate strategies to solve problems:</p> <ul style="list-style-type: none"> <li>• create a mathematical model</li> <li>• draw a picture</li> <li>• act it out</li> <li>• look for a pattern</li> <li>• guess and check</li> <li>• make an organized list</li> <li>• make a simpler but similar problem</li> </ul> <p><b><u>Reasoning and Proof</u></b></p> <p>1. Use models and logic to make conclusions. 2. Adjust models as needed. 3. Reason inductively by identifying patterns. 4. Evaluate and analyze the mathematical thinking and strategies of others, orally and in writing. 5. Include enough detail and clarity that the reader/listener can follow the explanation.</p> <p><b><u>Communication</u></b></p> <p>1. Use developmentally appropriate mathematical language and vocabulary. 2. Respond to instructions orally, visually and in writing as appropriate; e.g., tell, share, describe, demonstrate, compare, discuss, write. 3. Respond clearly with sufficient detail so that thinking can be understood. 4. Present thinking in a logical and organized in manner and explain to others how a problem was solved. 5. Read and reread all of the given information and instructions to ensure understanding; e.g., identify key information needed to solve the problem.</p> <p><b><u>Connections</u></b></p> <p>1. Use learning from one area of mathematics to understand another.</p>

Grade 1 Indicators	Grade 2 Indicators	Grade 3 Indicators
<ul style="list-style-type: none"> <li>• graphical</li> </ul> <p>2. Understand that more than one representation can be used to appropriately represent the same mathematical idea or situation.</p> <p><u>Reflection</u></p> <p>1. Reflect on mathematical concepts that have been learned using drawings, pictures and/or words: e.g., as a class group discussion and activity, create a simple classroom chart to show what has been learned.</p> <p>2. In a math journal reflect on mathematical concepts that have been learned using drawings, pictures and/or words given writing prompts such as:</p> <ul style="list-style-type: none"> <li>• What did you do in math today?</li> <li>• What did you learn in math today?</li> <li>• What are some of the math words you used today?</li> </ul>	<p><u>Representation</u></p> <p>1. Select an appropriate representation of a mathematical idea or situation:</p> <ul style="list-style-type: none"> <li>• physical model/manipulative</li> <li>• picture/drawing/diagram</li> <li>• numerical</li> <li>• geometric</li> <li>• graphical</li> <li>• table/chart</li> </ul> <p>2. Understand that more than one representation can be used to appropriately represent the same mathematical idea or situation.</p> <p>3. Use multiple representations, as required; e.g., table/chart, graph.</p> <p><u>Reflection</u></p> <p>1. Reflect on mathematical concepts that have been learned using drawings, pictures and/or words: e.g., as a class group discussion and activity, create a simple classroom chart to show what has been learned.</p> <p>2. In a math journal reflect on mathematical concepts that have been learned using drawings, pictures and/or words given writing prompts such as:</p> <ul style="list-style-type: none"> <li>• What did you do in math today?</li> <li>• What did you learn in math today?</li> <li>• Was what you learned easy or difficult?</li> <li>• What did you like or dislike about today's lesson?</li> <li>• What are some of the math words you used today?</li> </ul>	<p>2. Relate new and prior knowledge to make sense of new concepts being learned.</p> <p>3. Make connections between mathematics and everyday life.</p> <p>4. Apply a strategy or reference system that draws on previous learning in another context.</p> <p>5. Make connections between different representations; e.g., numeric, graphical, and/or algebraic.</p> <p><u>Representation</u></p> <p>1. Select an appropriate representation of a mathematical idea or situation:</p> <ul style="list-style-type: none"> <li>• physical model/manipulative</li> <li>• picture/drawing/diagram</li> <li>• numerical</li> <li>• geometric</li> <li>• graphical</li> <li>• table/chart</li> <li>• graphical organizers/Venn diagram</li> </ul> <p>2. Understand that more than one representation can be used to appropriately represent the same mathematical idea or situation.</p> <p>3. Use multiple representations, as required; e.g., table/chart, graph.</p> <p><u>Reflection</u></p> <p>1. Reflect on mathematical concepts that have been learned using drawings, pictures and/or words: e.g., as a class group discussion and activity, create a simple classroom chart to show what has been learned.</p> <p>2. In a math journal reflect on mathematical concepts that have been learned using drawings, pictures, math symbols, vocabulary, and language appropriate to the topic. Use writing prompts such as:</p> <ul style="list-style-type: none"> <li>• What did you do in math today?</li> <li>• What did you learn in math today?</li> <li>• Was what you learned easy or difficult?</li> <li>• What did you like or dislike about today's lesson?</li> <li>• What are some of the math words you used today?</li> </ul>

Grade 1 Indicators	Grade 2 Indicators	Grade 3 Indicators
		<ul style="list-style-type: none"><li>• Describe uses for what you learned in math today.</li></ul>

## Numbers, Number Sense and Operations Standard

*Students demonstrate number sense, including an understanding of number systems and operations and how they relate to one another. Students compute fluently and make reasonable estimates using paper and pencil, technology-supported and mental methods.*

Grade 1 Indicators	Grade 2 Indicators	Grade 3 Indicators
<p>1. Represent whole numbers 0-100 and describe their <u>place value</u> using physical <u>models</u>, <u>numerals</u>, <u>words</u>, and <u>expanded notation</u>.</p> <p>2. Count forward and backward from 0 - 100, and count forward or backward starting at any number between 1 and 100. (Write numbers that come <u>before</u>, <u>after</u> or <u>in between</u> two given numbers)</p> <p>3. Read and write <u>numerals</u> 0 - 100.</p> <p>4. <u>Compare</u> and order numerals 0 -100, using mathematical language: <u>greater than</u>, <u>less than</u>, <u>equal to</u>.</p> <p>5. Identify <u>patterns</u> on a 100's chart and orally <u>skip count</u> by 10's, 5's and 2's, starting from 0 up to 100.</p> <p>6. Use <u>ordinal numbers</u> to identify and order objects up to 30 items.</p> <p>7. Recognize and classify numbers as <u>even</u> or <u>odd</u> by determining if a set of objects can be <u>shared equally</u> between two people (0 - 20).</p> <p>8. Model, represent and explain <u>addition</u> as <u>counting on</u> and <u>combining sets</u> using manipulatives, a number line, drawing pictures and a calculator.</p> <p>9. Use <u>strategies</u> for learning the basic addition facts for <u>sums</u> to 12; e.g., counting on, adding one more, adding two more, <u>doubles</u>, doubles plus or minus 1, making 10, adding zero, and missing <u>addends</u>.</p> <p>10. Model and use the commutative property for addition using manipulatives.</p> <p>11. Model, represent and explain <u>subtraction</u> as <u>comparison</u> and <u>take-away</u> using manipulatives, a number line, drawing pictures and a calculator.</p>	<p>1. Represent whole numbers 100-1,000 and describe their place value using physical <u>models</u>, <u>numerals</u>, <u>words</u>, and <u>expanded notation</u>.</p> <p>2. <u>Compare</u> and <u>order</u> numerals to 100 to 1,000, using mathematical language and symbols: <u>greater than</u>, <u>less than</u>, <u>equal to</u>, &gt;, &lt;, =.</p> <p>3. Recognize and classify numbers as <u>even</u> or <u>odd</u>: (0-100).</p> <p>4. Identify patterns on a 100's chart and orally <u>skip count</u> by 10's, 5's and 2's starting from any single digit number: e.g. 1, 11, 21, 31..., 5, 15, 25, 35... 1, 6, 11, 16 ..., 2, 7, 12, 17...</p> <p>5. <u>Round</u> 2-digit and 3-digit numbers to the nearest 10 and 100.</p> <p>6. Model, represent and explain <u>addition</u> and <u>subtraction</u> using manipulatives, a number line, drawing pictures and a calculator.</p> <p>7. Use strategies for learning the basic addition and subtraction facts for <u>sums</u> to 18; e.g., counting on or counting backwards, one more or one less, two more or two less, doubles, doubles plus or minus 1, making 10, adding zero, missing <u>addends</u>.</p> <p>8. Demonstrate fluency with addition and subtraction facts, sums to 18.</p> <p>9. Add and subtract 2-digit numbers with and without <u>regrouping</u>.</p> <p>10. Model and use the <u>commutative property</u> of addition using number sentences.</p>	<p>1. Represent whole numbers to <u>hundred thousands</u> place using physical models, numerals, words, and <u>expanded notation</u>.</p> <p>2. Compare and order numbers 1,000 to 1,000,000, using mathematical language and symbols: greater than, less than, equal to, &gt;, &lt;, =.</p> <p>3. <u>Round</u> 2, 3, and 4-digit numbers to the nearest 10, 100, or 1,000.</p> <p>4. Add and subtract 3-digit whole numbers with and without <u>regrouping</u>.</p> <p>5. <u>Estimate</u> the results of whole number addition and subtraction problems using <u>rounding</u>, and <u>front end estimation</u>, and judge the reasonableness.</p> <p>6. Model, represent and explain the meaning of <u>multiplication</u>; e.g., <u>repeated addition</u>, skip counting, rectangular <u>arrays</u>.</p> <p>7. Model, represent and explain the meaning of <u>division</u>; e.g., <u>repeated subtraction</u>, separating a large group of items into smaller equal groups.</p> <p>8. Develop multiplication and division facts to the 12's.</p> <p>9. Explain and use relationships between operations such as addition and subtraction are <u>inverse</u> operations, and multiplication and division are inverse operations; e.g., fact families.</p> <p>10. Mentally compute with <u>multiples</u> of 10; e.g., 30 x 5, 40 x 60, 200 x 9</p> <p>11. Multiply 2-digit numbers by a single digit number.</p> <p>12. Divide numbers with <u>remainders</u>; e.g. <math>12 \div 5 =</math>, <math>25 \div 6</math> (digit single quotients).</p>

Grade 1 Indicators	Grade 2 Indicators	Grade 3 Indicators
<p>12. Use strategies for learning the basic subtraction facts for sums to 12; e.g., counting back, counting up from the number being subtracted, one less, two less.</p> <p>13. Explain the relationship between operations such as subtraction is the inverse of addition; e.g., <u>fact families</u> to 12.</p> <p>14. Add and subtract <u>2-digit numbers</u> - no regrouping; e.g., using base 10 blocks, dimes and pennies, paper and pencil.</p> <p>15. <u>Estimate</u> and solve problems involving addition and subtraction through the use manipulatives, pictures, drawings, and conventional <u>symbols</u>.</p> <p>16. Model, and represent multiplication as combining <u>equal groups</u>.</p> <p>17. Model and represent division as <u>sharing equally</u>.</p> <p>18. Use a variety of methods and tools to compute, including objects, mental computation, estimation, paper and pencil, and calculators.</p> <p>19. Represent commonly used <u>fractions</u> using physical models, pictures and words: <u>halves</u> (1/2, 2/2), <u>thirds</u> (1/3, 2/3, 3/3), <u>fourths</u> (1/4, 2/4, 3/4, 4/4).</p> <p>20. Compare halves, thirds, and fourths, using physical models.</p> <p>21. Identify and state the value of a <u>penny</u>, <u>nickel</u>, <u>dime</u>, <u>quarter</u>, <u>half dollar</u>, and <u>dollar</u>.</p> <p>22. Count coin sets with values up to \$1.00 using 1 or 2 different types of coins, consisting of pennies, nickels, dimes or quarters.</p> <p>23. Show different coin exchanges for the same amount; e.g., show \$.35 as a quarter and a dime, 3 dimes and 1 nickel, or 7 nickels.</p>	<p>11. Explain the relationship between operations such as subtraction is the inverse of addition; e.g., <u>fact families</u> to 18.</p> <p>12. Model, and represent <u>multiplication</u> as <u>combining equal groups</u> and as <u>repeated addition</u>.</p> <p>13. Model and represent <u>division</u> as <u>sharing equally</u>, and as <u>repeated subtraction</u>.</p> <p>14. Estimate the results of whole number addition and subtraction problems, using <u>rounding</u> and <u>front end estimation</u>, and judge the reasonableness.</p> <p>15. Use a variety of methods and tools to compute, including objects, mental computation, estimation, paper and pencil, and calculators.</p> <p>16. Represent commonly used <u>fractions</u> using physical models, pictures, numerals and words: <u>halves</u>, <u>thirds</u>, <u>fourths</u>, <u>sixths</u>, <u>eighths</u>.</p> <p>17. Identify and illustrate fractions as parts of a <u>whole</u>, and parts of a <u>set</u> of objects.</p> <p>18. Compare and describe commonly used fractions using models: halves, thirds, fourths, eighths.</p> <p>19. Count coin sets using any combination of coins consisting of <u>pennies</u>, <u>nickels</u>, <u>dimes</u>, <u>quarters</u> and <u>half dollars</u>, and write the values using a <u>cent sign</u> and in decimal form using a <u>dollar sign</u>.</p> <p>20. Count money sets consisting of coins and bills up to \$5.00.</p> <p>21. Make <u>change</u> using coins and a dollar bill.</p>	<p>13. Divide 2 digit numbers by a single digit number, without remainders.</p> <p>14. Model and use the <u>commutative</u> and <u>associative</u> properties for addition and multiplication using number sentences.</p> <p>15. Represent <u>fractions</u> and <u>mixed numbers</u> using physical models, numerals, and words:</p> <p>16. Compare and order commonly used fractions using physical or visual models; e.g. fraction circles or bars, number lines.</p> <p>17. Explore <u>equivalent</u> forms of fractions found by using physical models and visual models.</p> <p>18. Represent <u>decimal numbers</u> for <u>tenths</u> and <u>hundredths</u> using physical or visual models, numerals and words, and be able to write the fraction equivalents; e.g., 0.2, 2/10, two tenths.</p> <p>19. Count money using coins and bills to ten dollars.</p> <p>20. Make change using coins and bills for amounts up to \$5.00.</p> <p>21. Add and subtract decimals and amounts of money.</p> <p>22. Explore numbers less than 0 by extending the number line and through familiar applications; e.g., temperature.</p>

# Measurement Standard

*Students estimate and measure to a required degree of accuracy and precision by selecting and using appropriate units, tools and technologies.*

Grade 1	Grade 2	Grade 3
<ol style="list-style-type: none"> <li>1. Estimate and measure <u>length</u> using non-standard units; e.g., student foot, paper clips.</li> <li>2. Estimate and measure length using standard units; e.g., <u>inches, feet, centimeters</u>.</li> <li>3. Recognize and explain the need for standard units and tools for measuring length and weight; e.g., <u>rulers</u> and <u>balance scales</u>.</li> <li>4. Recognize the attributes of <u>length, capacity, weight, and time</u>.</li> <li>5. Estimate and measure weight using non-standard units; e.g., blocks of uniform size, a book.</li> <li>6. Estimate and measure capacity using non-standard units; e.g., small paper cups,</li> <li>7. Select an appropriate unit and tool for the attribute being measured.</li> <li>8. Relate the number of units required to the size of units; e.g., a smaller unit requires more, a larger unit requires less.</li> <li>9. Recognize the reasonableness of a measurement.</li> <li>10. Order a <u>sequence</u> of events with respect to time; e.g., seasons of the year; morning, afternoon and night.</li> <li>11. Tell time to the <u>hour</u> and <u>half-hour</u> using digital and analog clocks.</li> </ol>	<ol style="list-style-type: none"> <li>1. Identify and select appropriate <u>customary</u> and <u>metric</u> units for measuring <u>length</u>; <u>inches, feet, yards, centimeters, meters</u> and recognize the abbreviations.</li> <li>2. Use inches and centimeters to measure length; e.g., use a ruler to measure common objects, and to draw line segments using inches, half inches, and centimeters.</li> <li>3. Identify and select appropriate units of measure for customary and metric <u>capacity</u>; <u>cups, pints, quarts, liters</u> and recognize the abbreviations.</li> <li>4. Use cups and liters to measure capacity; e.g., use a measuring cup to place 2 cups of rice in a bowl.</li> <li>5. Identify and select appropriate customary and metric units for measuring weight; <u>ounces, pounds, grams</u> and recognize the abbreviations.</li> <li>6. Use pounds and grams to measure weight; e.g., use a scale to weigh 50 grams of candy or 1 lb. of candy.</li> <li>7. Establish personal or common referents for units of measure to make estimates and comparisons; e.g., the width of a pinky finger is about a cm, a large bottle of pop is 2 liters, a small paper clip is weighs about one gram.</li> <li>8. Estimate the length, capacity and weight of common objects using customary units and metric units.</li> <li>9. Tell time to <u>5 minute intervals</u> and to the <u>quarter hr.</u> using digital and analog clocks.</li> <li>10. Read and record <u>temperatures</u> in both <u>Fahrenheit</u> and <u>Celsius</u> degrees.</li> </ol>	<ol style="list-style-type: none"> <li>1. Identify and select appropriate <u>customary</u> and <u>metric</u> units for measuring <u>length</u>; <u>inches, feet, yards, miles, centimeters, decimeters, meters</u> and use abbreviations.</li> <li>2. Use a ruler to measure length to the nearest inch, <math>\frac{1}{2}</math> in., <math>\frac{1}{4}</math> in., centimeter, decimeter, meter; e.g., measure common objects; draw a rectangle with a length of <math>2\frac{1}{2}</math> in. and a width of 3 in.</li> <li>3. Identify and select appropriate <u>customary</u> and <u>metric</u> units for measuring <u>capacity</u>; <u>cups, pints, quarts, gallons, centiliters, deciliters, liters</u> and use abbreviations.</li> <li>4. Use cups, pints, quarts, gallons, centiliters, liters, to measure capacity; e.g., fill a measuring cup to the <math>\frac{3}{4}</math> cup mark.</li> <li>5. Identify and select appropriate <u>customary</u> and <u>metric</u> units for measuring <u>weight</u>; <u>ounces, pounds, tons, grams, kilograms</u> and use abbreviations.</li> <li>6. Use ounces, pounds, grams, and kilograms to measure weight; e.g., use a scale to weigh and compare common objects.</li> <li>7. Read thermometers in both <u>Fahrenheit</u> and <u>Celsius</u> scales.</li> <li>8. Establish personal or common referents for units of measure to make estimates and comparisons; a paper clip is approximately one gram, the width of a pinky finger is approximately one cm, four times around a football field is approximately one mile, the width of a doorway is approximately one yard.</li> <li>9. Tell time to the nearest minute using digital and analog clocks.</li> </ol>

Grade 1	Grade 2	Grade 3
		<p>10. Tell time using words; “before” and “after”, “<u>quarter to</u>”, “<u>quarter after</u>”.</p> <p>11. Calculate <u>elapsed time</u> using a clock (hrs. and half hours), and a calendar (days and weeks).</p> <p>12. Demonstrate and describe <u>perimeter</u> as distance around a shape; <u>area</u> as covering a two-dimensional shape; <u>volume</u> as filling a three-dimensional shape.</p> <p>13. Develop strategies for estimating the perimeters, areas, and volumes of regular and irregular shapes; e.g., links, tiles, cubes, grid paper.</p>

## Geometry and Spatial Sense Standard

*Students identify, classify, compare and analyze characteristics, properties and relationships of one-, two- and three-dimensional geometric figures and objects. Students use spatial reasoning, properties of geometric objects, and transformations to analyze mathematical situations and solve problems.*

Grade 1 Indicators	Grade 2 Indicators	Grade 3 Indicators
<p>1. Recognize <u>two-dimensional</u> geometric shapes in the environment; <u>circle, square, rectangle, triangles, or parallelogram</u>.</p> <p>2. Recognize <u>three-dimensional</u> structures in the environment; e.g., <u>cylinders, cones, spheres, cubes, rectangular prisms</u>.</p> <p>3. Copy figures and draw simple two-dimensional shapes from memory.</p> <p>4. Cover two-dimensional pictures or figures using paper shapes or <u>tangrams</u>.</p> <p>5. Describe two-dimensional shapes using attributes such as number of <u>sides</u> and number of <u>corners</u>.</p> <p>6. Build three-dimensional objects using blocks.</p> <p>7. Compare and sort two and three-dimensional shapes according to their <u>attributes</u>, then explain reasoning for the groupings and comparisons.</p> <p>8. Create new shapes by combining or cutting apart existing shapes.</p> <p>9. Identify the shapes of the <u>faces</u> of three-dimensional objects.</p> <p>10. Extend and use <u>location words</u> to include distance (<u>near, far, close to</u>) and directional words (<u>left, right</u>).</p>	<p>1. Identify and describe <u>two-dimensional</u> shapes; <u>circle, square, rectangle, triangle, parallelogram, rhombus, and trapezoid</u>.</p> <p>2. Identify <u>three-dimensional</u> objects as <u>cylinders, cones, spheres, cubes, rectangular prisms, pyramids</u>.</p> <p>3. Identify, compare, and sort <u>three-dimensional</u> objects according to the shape of the faces, the number of <u>faces</u>, number of <u>edges</u>, or number of <u>vertices</u>.</p> <p>4. Investigate and predict the results of putting together and taking apart two and three-dimensional shapes.</p> <p>5. Build a <u>three-dimensional</u> model based on an <u>illustration</u> or actual object using items such as legos, Lincoln logs, or wooden blocks.</p> <p>6. Recognize and apply <u>flips, slides and turns</u>.</p> <p>7. Recognize and create shapes that have <u>symmetry</u>.</p> <p>8. Identify two-dimensional shapes as <u>congruent</u> (same shape and same size), or <u>similar</u> (same shape, different size).</p>	<p>1. Analyze and describe properties of two-dimensional and three-dimensional objects using terms such as <u>vertex, edge, angle, side</u> and <u>face</u>.</p> <p>2. Build a <u>three-dimensional</u> model based on an <u>illustration</u> or actual object using items such as legos, Lincoln logs, or wooden blocks.</p> <p>3. Identify two-dimensional shapes as <u>congruent</u> or <u>similar</u>.</p> <p>4. Predict and describe the results of <u>sliding, flipping, and turning</u> two-dimensional shapes.</p> <p>5. Draw lines of <u>symmetry</u> to verify symmetrical two-dimensional shapes.</p> <p>6. Identify and describe <u>right angles</u>.</p> <p>7. Use physical models, such as straws, to create different sized <u>angles</u> by opening and closing the sides.</p> <p>8. Identify and draw <u>angles</u> with respect to right angles; <u>greater than 90°</u>, <u>less than 90°</u>, <u>equal to 90°</u>.</p> <p>9. Find and name locations on a labeled grid or <u>coordinate plane</u>.</p>

## Patterns, Functions and Algebra Standard

*Students use patterns, relations and functions to model, represent and analyze problem situations that involve variable quantities, Students analyze, model and solve problems using various representations such as tables, graphs and equations.*

Grade 1 Indicators	Grade 2 Indicators	Grade 3 Indicators
<p>1. Analyze, describe, and extend sequences of sounds, shapes or simple number patterns; e.g., AABBBabAABB...; <math>\square\square\triangle\triangle\square\square\triangle\dots</math> (Pattern blocks, attribute shapes); 1,3,1,3,...</p> <p>2. Describe orally the basic unit or general plan of a <u>repeating</u> or <u>growing pattern</u>.</p> <p>3. <u>Sort</u>, <u>classify</u>, and <u>order</u> objects by shape, size, number, and other properties and describe the <u>attributes</u> used; e.g., buttons, stickers, seashells.</p> <p>4. Identify and write a short sentence to describe the attribute that was used to sort a group of items that have already been sorted.</p> <p>5. Solve open sentences by representing an expression in more than one way using the commutative property; e.g., <math>4 + 5 = 5 + 4</math> or the number of blue blocks plus red blocks is the same as the number of red blocks plus the number of blue blocks (<math>r + b = b + r</math>).</p> <p>6. Describe orally and model a problem situation using objects, pictures, or number sentences.</p>	<p>1. Extend simple number patterns, both <u>repeating and growing patterns</u>.</p> <p>2. Use patterns to make generalizations and predictions; e.g., determine a <u>missing element</u> in a pattern.</p> <p>3. Create new patterns with consistent <u>rules</u> or <u>plans</u>.</p> <p>4. Describe the rule or general plan of existing patterns.</p> <p>5. Model a problem situation using objects, pictures, numbers and other symbols.</p> <p>6. Understand <u>equivalence</u> and extend the concept to situations involving symbols; e.g., <math>4 + 5 = 9</math> and <math>9 = 4 + 5</math>, and <math>4 + 5 = 3 + 6 = \Delta + \square</math>.</p> <p>7. Use symbols to represent <u>unknown quantities</u> and identify values for <u>symbols</u> in an <u>expression</u> or <u>equation</u> using addition and subtraction; e.g., <math>7 + \square = 10</math>; <math>\Delta - 2 = 5</math>.</p> <p>8. Describe <u>qualitative change</u>; e.g., a student growing taller.</p> <p>9. Describe <u>quantitative change</u>; e.g., a student growing two inches in one year.</p>	<p>1. Analyze and extend increasing <u>arithmetic (+) patterns</u>, with or without a calculator, and describe the rules in words; e.g., 4,7,10,13,...; 6,11,16,21,...</p> <p>2. Analyze and extend increasing <u>geometric (x) patterns</u>, with or without a calculator and describe the rule in words; e.g., 1,2,4,8,...; 1,3,9,27,...</p> <p>3. Use patterns to make predictions, identify relationships, and solve problems.</p> <p>4. Write, solve, and explain simple mathematical statements, such as <math>7 + \square &gt; 8</math> or <math>\Delta + 8 = 12</math>.</p> <p>5. Create tables to discover patterns and rules; e.g., <u>input/output tables</u>.</p> <p>6. Model problem situations using objects, pictures, tables, numbers, letters and other symbols.</p> <p>7. Express mathematical relationships as <u>equations</u> and <u>inequalities</u>.</p> <p>8. Identify and describe <u>quantitative changes</u>, especially those involving addition and subtraction; e.g., the heights of water in a glass becoming 1 centimeter lower each week due to evaporation.</p> <p>9. Investigate ways a change in one <u>variable</u> relates to a change in a second variable by simulating an input/output machine; e.g., “x +12 machine” means if 8 goes in 20 comes out, or 1 sandwich costs \$0.99, so 2 cost _____?</p>

## Data Analysis and Probability Standard

*Students pose questions and collect, organize, represent, interpret and analyze data to answer those questions. Students develop and evaluate inferences, predictions and arguments that are based on data.*

Grade 1 Indicators	Grade 2 Indicators	Grade 3 Indicators
<p>1. Collect data about everyday situations and familiar objects and organize into <u>tables</u> and <u>charts</u> using <u>tally marks</u>; e.g., data collected from <u>surveys</u> (favorite pets, favorite foods) and data collected over a period of time.</p> <p>2. Identify <u>multiple categories</u> for sorting objects and data.</p> <p>3. Display collected data in <u>bar graphs</u> and <u>picture graphs</u> with intervals of 1.</p> <p>4. Read and interpret information on <u>charts</u> and <u>graphs</u>; e.g. answer questions about the number of objects represented in a <u>picture graph</u>, <u>bar graph</u> or <u>table</u>; how many more in a category compared to another, or how many altogether in two categories.</p> <p>5. Construct a question that can be answered by using information from a graph.</p> <p>6. Read and use <u>time lines</u> to display a <u>sequence</u> of events.</p> <p>7. Discuss and describe the likelihood of simple events as <u>possible/impossible</u> and <u>more likely/less likely</u>; e.g., when using spinners or number cubes in classroom activities.</p>	<p>1. Pose questions and collect data through <u>observations</u>, <u>interviews</u> and <u>surveys</u>.</p> <p>2. Organize data into <u>tables</u> and <u>charts</u> using <u>tally marks</u>.</p> <p>3. Display collected data in picture graphs with units of 1 or 2 and <u>bar graphs</u> and <u>line plots</u> with intervals of 1 or 2.</p> <p>4. Recognize that data may vary from one <u>population</u> to another; e.g., favorite foods or favorite TV shows of parents and students.</p> <p>5. Read, interpret, compare, and make predictions from data represented in <u>charts</u>, <u>tables</u>, <u>bar graphs</u>, <u>picture graphs</u> and <u>line plots</u>.</p> <p>6. Write sentences to describe and compare categories of data represented in a chart or graph, and make statements about the data as a whole.</p> <p>7. Read, use and construct <u>time lines</u> to display a <u>sequence</u> of events.</p> <p>8. Identify <u>untrue</u> or <u>inappropriate</u> statements about a given set of data.</p> <p>9. List some of the possible <u>outcomes</u> of a simple experiment, and predict whether given outcomes are <u>more</u>, <u>less</u>, or <u>equally likely</u> to occur.</p> <p>10. Use physical models and pictures to represent possible <u>arrangements</u> of 2 or 3 objects.</p>	<p>1. Collect and organize data from an experiment, such as recording and classifying observations or measurements in response to a question posed.</p> <p>2. Interpret and construct <u>picture graphs</u> in which a symbol or picture represents more than one object.</p> <p>3. Interpret and construct <u>bar graphs</u> with intervals greater than one; e.g., intervals of 2, 5, or 10.</p> <p>4. Support a <u>conclusion</u> orally and in writing, using information in a table or a graph.</p> <p>5. Match a set of data with a <u>graphical representation</u> of that data.</p> <p>6. Fluently translate data among <u>charts</u>, <u>tables</u>, <u>line plots</u>, <u>picture graphs</u>, and <u>bar graphs</u>.</p> <p>7. Analyze and interpret information represented on a <u>time line</u>.</p> <p>8. Identify the <u>mode</u> of a data set and describe the information it gives about the data set.</p> <p>9. Conduct a simple experiment, record the results in a chart, table or graph. Use results to draw conclusions about <u>possible outcomes</u>.</p> <p>10. Use physical models, pictures, diagrams, and lists to solve problems involving possible <u>arrangements</u> or <u>combinations</u> of two to four objects.</p>